

Princeton Talk on Objects

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Syntax

Records

$A, B ::=$	type
$[l_i v_i : B_i]_{i \in 1..n}$	record type ($v_i \in \{-, ^\circ, +\}$, l_i distinct)
$a, b ::=$	term
$[l_i = b_i]_{i \in 1..n}$	record (l_i distinct)
$a.l$	field selection
$a.l := b$	field update

Simple Objects

$A, B ::=$	type
$[l_i v_i : B_i]_{i \in 1..n}$	object type ($v_i \in \{-, ^\circ, +\}$, l_i distinct)
$a, b ::=$	term
$[l_i = \zeta(x_i : A) b_i]_{i \in 1..n}$	object (l_i distinct)
$a.l$	method invocation
$a.l \Leftarrow \zeta(x : A) b$	method override
$\text{clone}(a)$	cloning

Object with Self

$A, B ::=$	type
$\text{Obj}(X)[l_i v_i : B_i \{X\}]_{i \in 1..n}$	object type ($v_i \in \{-, ^\circ, +\}$, l_i distinct)
$a, b ::=$	term
$\text{obj}(X=A)[l_i = \zeta(x_i : X) b_i]_{i \in 1..n}$	object (l_i distinct)
$a.l$	method invocation
$a.l \Leftarrow \zeta(Y <: A, x : Y) b$	method override
$\text{clone}(a)$	cloning

Ambient Syntax

$A, B ::= \dots$	type
X	type variable
Top	maximum type
$\forall(X<:A)B$	bounded universal type
$a, b ::= \dots$	term
x	variable
$\lambda(X<:A)b$	type abstraction
$b(A)$	type application
$\text{let } x:A=a \text{ in } b$	call-by-value let

Field Notation: $[\dots] = b \dots$ stands for $\text{let } y:?=b \text{ in } [\dots] = \zeta(x)y \dots$ with $y \notin b$
 $a.l = b$ stands for $\text{let } y:?=b \text{ in } a.l \Leftarrow \zeta(x)y$ with $y \notin b$

Functions: are definable

Type Rules

Judgments

$E \vdash \diamond$	well-formed environment judgment
$E \vdash A$	type judgment
$E \vdash A <: B$	subtyping judgment
$E \vdash v_1 A <: v_2 B$	component subtyping judgment
$E \vdash a : A$	value typing judgment

Ambient Type Theory

(Env \emptyset)	(Env x)	(Env X)
$\frac{}{\emptyset \vdash \diamond}$	$\frac{}{E \vdash A \quad x \notin \text{dom}(E)} E, x:A \vdash \diamond$	$\frac{}{E \vdash A \quad X \notin \text{dom}(E)} E, X<:A \vdash \diamond$

(Type X)	(Type Top)	(Type \forall)
$\frac{}{E', X<:A, E'' \vdash \diamond}$	$\frac{}{E \vdash \diamond} E \vdash \text{Top}$	$\frac{}{E, X<:A \vdash B} E \vdash \forall(X<:A)B$

(Sub Refl)	(Sub Trans)	(Sub X)	(Sub Top)	(Sub \forall)
$\frac{}{E \vdash A} E \vdash A <: A$	$\frac{}{E \vdash A <: B \quad E \vdash B <: C} E \vdash A <: C$	$\frac{}{E', X<:A, E'' \vdash \diamond} E', X<:A, E'' \vdash X <: A$	$\frac{}{E \vdash A} E \vdash A <: \text{Top}$	$\frac{}{E \vdash A' <: A \quad E, X<:A' \vdash B <: B'} E \vdash \forall(X<:A)B <: \forall(X<:A')B'$

(Val Subsumption)	(Val x)
$\frac{}{E \vdash a : A \quad E \vdash A <: B} E \vdash a : B$	$\frac{}{E', x:A, E'' \vdash \diamond} E', x:A, E'' \vdash x:A$
(Val Fun2)	(Val App12)
$\frac{}{E, X<:A \vdash b : B} E \vdash \lambda(b) : \forall(X<:A)B$	$\frac{}{E \vdash a : \forall(X<:A)B\{X\} \quad E \vdash A' <: A} E \vdash a() : B\{A'\}$
(Val Let)	
$\frac{}{E \vdash a : A \quad E, x:A \vdash b : B} E \vdash \text{let } x:A=a \text{ in } b : B$	

Records

(Type Record) (l_i distinct)

$$\frac{E \vdash B_i \quad \forall i \in 1..n}{E \vdash [l_i v_i : B_i]_{i \in 1..n}}$$

$$E \vdash [l_i v_i : B_i]_{i \in 1..n}$$

(Sub Record) (l_i distinct)

$$\frac{E \vdash v_i B_i <: v_i' B_i' \quad \forall i \in 1..n}{E \vdash [l_i v_i : B_i]_{i \in 1..n+m} <: [l_i v_i' : B_i']_{i \in 1..n}}$$

$$E \vdash [l_i v_i : B_i]_{i \in 1..n+m} <: [l_i v_i' : B_i']_{i \in 1..n}$$

(Sub Invariant)

$$\frac{E \vdash B}{E \vdash \circ B <: \circ B}$$

(Sub Covariant)

$$\frac{E \vdash B <: B' \quad v \in \{^{\circ}, +\}}{E \vdash v B <: + B'}$$

(Sub Contravariant)

$$\frac{E \vdash B' <: B \quad v \in \{^{\circ}, -\}}{E \vdash v B <: - B'}$$

$$E \vdash \circ B <: \circ B$$

$$E \vdash v B <: + B'$$

$$E \vdash v B <: - B'$$

(Val Record) (l_i distinct)

(where $A \equiv [l_i v_i : B_i]_{i \in 1..n}$)

$$\frac{E \vdash b_i : B_i \quad \forall i \in 1..n}{E \vdash [l_i = b_i]_{i \in 1..n} : A}$$

$$E \vdash [l_i = b_i]_{i \in 1..n} : A$$

(Val Record Select)

$$\frac{E \vdash a : [l_i v_i : B_i]_{i \in 1..n} \quad v_j \in \{^{\circ}, +\} \quad j \in 1..n}{E \vdash a.l_j : B_j}$$

$$E \vdash a.l_j : B_j$$

(Val Record Update)

(where $A' \equiv [l_i v_i : B_i]_{i \in 1..n}$)

$$\frac{E \vdash a : A \quad E \vdash A <: A' \quad E \vdash b : B_j \quad v_j \in \{^{\circ}, -\} \quad j \in 1..n}{E \vdash a.l_j := b : A}$$

$$E \vdash a.l_j := b : A$$

Simple Objects

(Type Simple Object) (l_i distinct)

$$\frac{E \vdash B_i \quad \forall i \in 1..n}{E \vdash [l_i v_i : B_i]_{i \in 1..n}}$$

$$E \vdash [l_i v_i : B_i]_{i \in 1..n}$$

(Sub Simple Object) (l_i distinct)

$$\frac{E \vdash v_i B_i <: v_i' B_i' \quad \forall i \in 1..n}{E \vdash [l_i v_i : B_i]_{i \in 1..n+m} <: [l_i v_i' : B_i']_{i \in 1..n}}$$

$$E \vdash [l_i v_i : B_i]_{i \in 1..n+m} <: [l_i v_i' : B_i']_{i \in 1..n}$$

(Sub Invariant)

$$\frac{E \vdash B}{E \vdash \circ B <: \circ B}$$

(Sub Covariant)

$$\frac{E \vdash B <: B' \quad v \in \{^{\circ}, +\}}{E \vdash v B <: + B'}$$

(Sub Contravariant)

$$\frac{E \vdash B' <: B \quad v \in \{^{\circ}, -\}}{E \vdash v B <: - B'}$$

$$E \vdash \circ B <: \circ B$$

$$E \vdash v B <: + B'$$

$$E \vdash v B <: - B'$$

(Val Simple Object) (l_i distinct)

(where $A \equiv [l_i v_i : B_i]_{i \in 1..n}$)

$$\frac{E, x_i : A \vdash b_i : B_i \quad \forall i \in 1..n}{E \vdash [l_i = \zeta(x_i : A) b_i]_{i \in 1..n} : A}$$

$$E \vdash [l_i = \zeta(x_i : A) b_i]_{i \in 1..n} : A$$

(Val Simple Object Select)

$$\frac{E \vdash a : [l_i v_i : B_i]_{i \in 1..n} \quad v_j \in \{^{\circ}, +\} \quad j \in 1..n}{E \vdash a.l_j : B_j}$$

$$E \vdash a.l_j : B_j$$

(Val Simple Object Override)

(where $A' \equiv [l_i v_i : B_i]_{i \in 1..n}$)

$$\frac{E \vdash a : A \quad E \vdash A <: A' \quad E, x : A \vdash b : B_j \quad v_j \in \{^{\circ}, -\} \quad j \in 1..n}{E \vdash a.l_j \Leftarrow \zeta(x : A) b : A}$$

$$E \vdash a.l_j \Leftarrow \zeta(x : A) b : A$$

(Val Simple Object Clone)

(where $A' \equiv [l_i v_i : B_i]_{i \in 1..n}$)

$$\frac{E \vdash a : A \quad E \vdash A <: A'}{E \vdash \text{clone}(a) : A}$$

$$E \vdash \text{clone}(a) : A$$

Objects with Self

(Type Object) (I_i distinct) ($B\{X^+\} \triangleq B$ covariant in X)

$$\frac{E, X \prec: \text{Top} \vdash B_i\{X^+\} \quad \forall i \in 1..n}{E \vdash \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n}}$$

$$E \vdash \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n}$$

(Sub Object) (I_i distinct)

$$\frac{E, Y \prec: \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n+m} \vdash \nu_i B_i\{Y\} \prec: \nu_i' B_i'\{Y\} \quad \forall i \in 1..n}{E \vdash \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n+m} \prec: \text{Obj}(X)[I_i \nu_i' : B_i'\{X\}]^{i \in 1..n}}$$

$$E \vdash \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n+m} \prec: \text{Obj}(X)[I_i \nu_i' : B_i'\{X\}]^{i \in 1..n}$$

(Sub Invariant)

(Sub Covariant)

(Sub Contravariant)

$$\frac{E \vdash B}{E \vdash \circ B \prec: \circ B}$$

$$\frac{E \vdash B \prec: B'}{E \vdash \nu B \prec: + B'}$$

$$\frac{E \vdash B' \prec: B \quad \nu \in \{^{\circ}, +\}}{E \vdash \nu B' \prec: - B'}$$

$$E \vdash \circ B \prec: \circ B$$

$$E \vdash \nu B \prec: + B'$$

$$E \vdash \nu B' \prec: - B'$$

(Val Object) (I_i distinct) (where $A \equiv \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n}$)

$$\frac{E, x_i : A \vdash b_i\{A\} : B_i\{A\} \quad \forall i \in 1..n}{E \vdash \text{obj}(X=A)[I_i = \zeta(x_i : X) b_i\{X\}]^{i \in 1..n} : A}$$

$$E \vdash \text{obj}(X=A)[I_i = \zeta(x_i : X) b_i\{X\}]^{i \in 1..n} : A$$

(Val Select)

(where $A' \equiv \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n}$)

$$\frac{E \vdash a : A \quad E \vdash A \prec: A' \quad \nu_j \in \{^{\circ}, +\} \quad j \in 1..n}{E \vdash a.l_j : B_j\{A\}}$$

$$E \vdash a.l_j : B_j\{A\}$$

(Val Override)

(where $A' \equiv \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n}$)

$$\frac{E \vdash a : A \quad E \vdash A \prec: A' \quad E, Y \prec: A, x : Y \vdash b\{Y, x\} : B_j\{Y\} \quad \nu_j \in \{^{\circ}, -\} \quad j \in 1..n}{E \vdash a.l_j \Leftarrow \zeta(Y \prec: A, x : Y) b\{Y, x\} : A}$$

$$E \vdash a.l_j \Leftarrow \zeta(Y \prec: A, x : Y) b\{Y, x\} : A$$

(Val Clone)

(where $A' \equiv \text{Obj}(X)[I_i \nu_i : B_i\{X\}]^{i \in 1..n}$)

$$\frac{E \vdash a : A \quad E \vdash A \prec: A'}{E \vdash \text{clone}(a) : A}$$

$$E \vdash \text{clone}(a) : A$$

Variations for ML2000

1) Records/Objects components may be permutable (multiple subtyping) or non permutable (prefix subtyping). The latter allows direct access. The former allows practically-constant-time access, but with a factor of 3-5 in performance.

2) Subsumption of invariant components into covariant components may be allowed (enables “write-protection” of fields after initial definition) or forbidden (allows better compiler flow analysis).

3) Fields should be separated from methods, instead of being regarded as encoded from methods (otherwise fields can be overridden with methods and vice versa). This is necessary to allow fast access to fields. It is not clear, though, what is the best place to make this distinction, along the path between surface syntax and code generation.

Encoding of Class Types

TOOPL style:

Requires F-bounded quantification and recursive types, but only simple objects. Allows binary methods. Causes widespread loss of subsumption. The latter can be remedied by F-bounded matching, but the effect is to force widespread F-bounded parameterization.

Objects-with-Self style:

Requires ordinary bounded quantification and built-in Self types. Disallows binary methods, requiring them to be defined as binary functions. (Actually, binary methods can still be emulated by recursive types; this may be satisfactory in practice.) Causes no loss of subsumption.

TOOPL style

$A \equiv \text{ObjectType}(X)[l_i v_i; B_i \{X\}^{i \in 1..n}] \triangleq \mu(X)[l_i v_i; B_i \{X\}^{i \in 1..n}]$

$A(C) \triangleq [l_i v_i; B_i \{C\}^{i \in 1..n}]$

$\text{ClassType}(X)[l_i v_i; B_i \{X\}^{i \in 1..n}] \triangleq [\text{new}: A, l_i: \forall(X <: A(X)) X \rightarrow B_i \{X\}]$

Objects-with-Self style

$A \equiv \text{ObjectType}(X)[l_i v_i; B_i \{X^+\}^{i \in 1..n}] \triangleq \text{Obj}(X)[l_i v_i; B_i \{X^+\}^{i \in 1..n}]$

$\text{ClassType}(X)[l_i v_i; B_i \{X^+\}^{i \in 1..n}] \triangleq [\text{new}: A, l_i: \forall(X <: A) X \rightarrow B_i \{X\}]$

In either style one can define classes (members of `ClassTypes`) and subclasses that reuse or override methods of superclasses. The Objects-with-Self style may in fact be used together with simple recursive definitions to support binary methods, but without possibility to inherit them.

Compatibility of Subtyping and Method Overriding

When does this inclusion hold?

$\text{ObjectType}(X)[l_i v_i; B_i \{X\}^{i \in 1..n+m}] <: \text{ObjectType}(X)[l_i v_i'; B_i' \{X\}^{i \in 1..n}]$

(1) In Objects-with-Self style (by the rules of object types with Self) it holds if:

$X <: \text{ObjectType}(X)[l_i v_i; B_i \{X^+\}^{i \in 1..n+m}]$ implies $v_i B_i \{X^+\} <: v_i' B_i' \{X^+\}$

Morale: subtyping is incompatible with method overriding for methods whose types contain contravariant occurrences of Self types (binary methods). However, covariant occurrences of Self types cause no problems, since the inclusion above is easily satisfied.

(2) In TOOPL-style (by the rules for μ and simple objects) it holds if:

$X <: Y$ implies $v_i B_i \{X\} <: v_i' B_i' \{Y\}$

This condition can be further analyzed as follows:

If X, Y occur in matching contravariant positions (binary methods), the requirement is $Y <: X$, hence there can be no inclusion. So let's assume there are only covariant occurrences.

If $v_i \equiv v_i' \equiv \circ$ then we have inclusion only if $B_i \{X^+\} \equiv B_i' \{Y^+\}$, that is if X, Y do not occur at all. In this case we can have inclusion and method override, but the types of the overridden methods cannot contain any instance of the Self type.

If $v_i \equiv v_i' \equiv +$ then we have inclusion if $B_i \{X^+\} <: B_i' \{Y^+\}$; matching occurrences of X, Y cause no problem. Here we can have inclusions, but method overriding is precluded by $v_i \equiv v_i' \equiv +$.

Morale: subtyping is incompatible with method overriding for methods whose types contain Self types, either contravariantly or covariantly.

Motivations for Objects with Self

The motivations for moving from simple object to objects with self are:

- 1) Full support for delegation (i.e. overriding even methods that return self, as just explained.)
- 2) Disallowing contravariant occurrences of Self, so that subsumption is not impeded. (Actually, one can still code binary methods, and impede subsumption, "by hand" with recursive definitions. However, these binary methods, unlike in TOOPL-style, cannot then be easily inherited.)
- 3) Removing the need for F-bounded quantification, and the associated need for equality of recursive types up to unfolding. That is, simplifying the necessary ambient type theory.

Laws

- 1) Subsumption is good: it should not be impeded.
 - 2) Self is good, provided it does not impede (1).
 - 3) Delegation is good provided it does not impede (1,2).
- No other features shall impede (1,2,3).

N.B. the popular “Inheritance is not subtyping” view favors binary methods and F-bounded quantification over subsumption and bounded quantification.

Expectations:

Class-based languages will evolve into delegation-based languages, because the latter are both simpler and more powerful.

Class mechanisms can be derived from delegation mechanisms, in a sufficiently rich ambient type theory.

Therefore, class and delegation mechanisms can be smoothly integrated in a delegation-based framework.

Class and Prototyping Constructs

$A, B ::=$	<i>Bonus</i>
$X, A \rightarrow B$	$\forall (X <: A) B$
$\text{Object}(X)[l_i v_i; B_i \{X^+\}^{ieI}]$	variance annotations
$\text{Class}(X)[l_i v_i; B_i \{X^+\}^{ieI}]$	
$a, b ::=$	<i>Bonus</i>
$x, \lambda(x:A)b, b(a)$	$\lambda(X <: A) B, b(A)$
$\text{class } (x:X <: A) l_i = b_i^{ieI} \text{ end}$	
$\text{extend } a \text{ with } (x:X <: A) l_i = b_i^{ieI} \text{ end}$	
$\text{override } a \text{ by } (x:X <: A) l_i = b_i^{ieI} \text{ end}$	
$\text{new}(a)$	$\text{object } (x:X=A) l_i = b_i^{ieI} \text{ end}$
$a.l$	
$a \text{ gets } [l_i = b_i^{ieI}]$	$\text{modify } a \text{ by } (x:X <: A) l_i = b_i^{ieI} \text{ end}$

Class-based

Prototype-based

N.B. Both features are available when adopting Objects withSelf.